

Question

- (a) Show that the equation

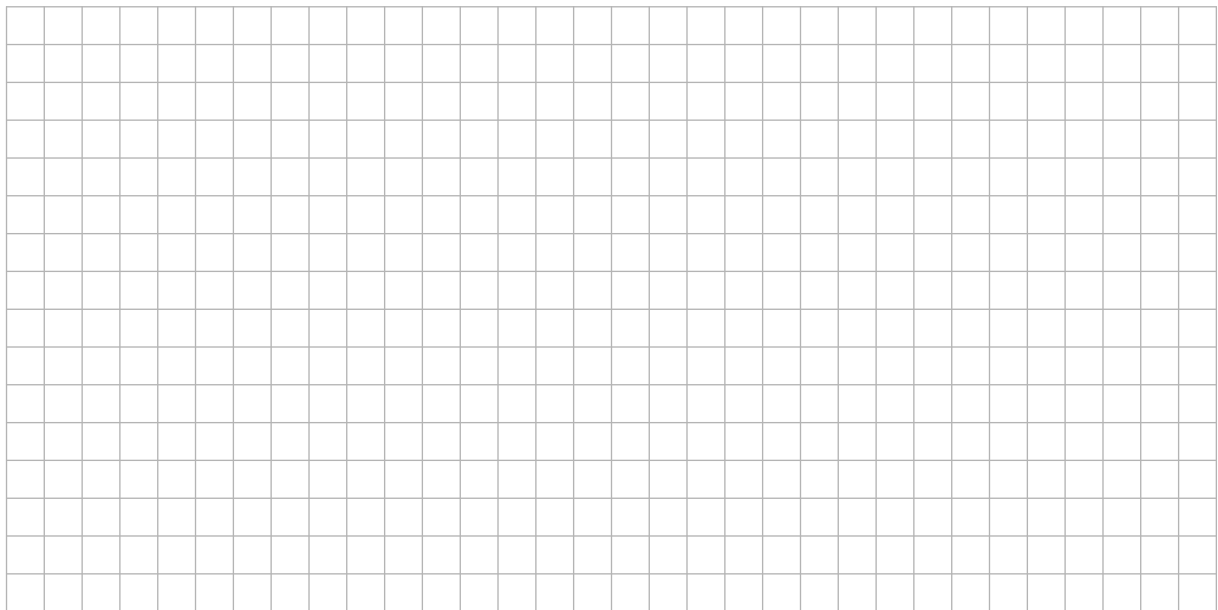
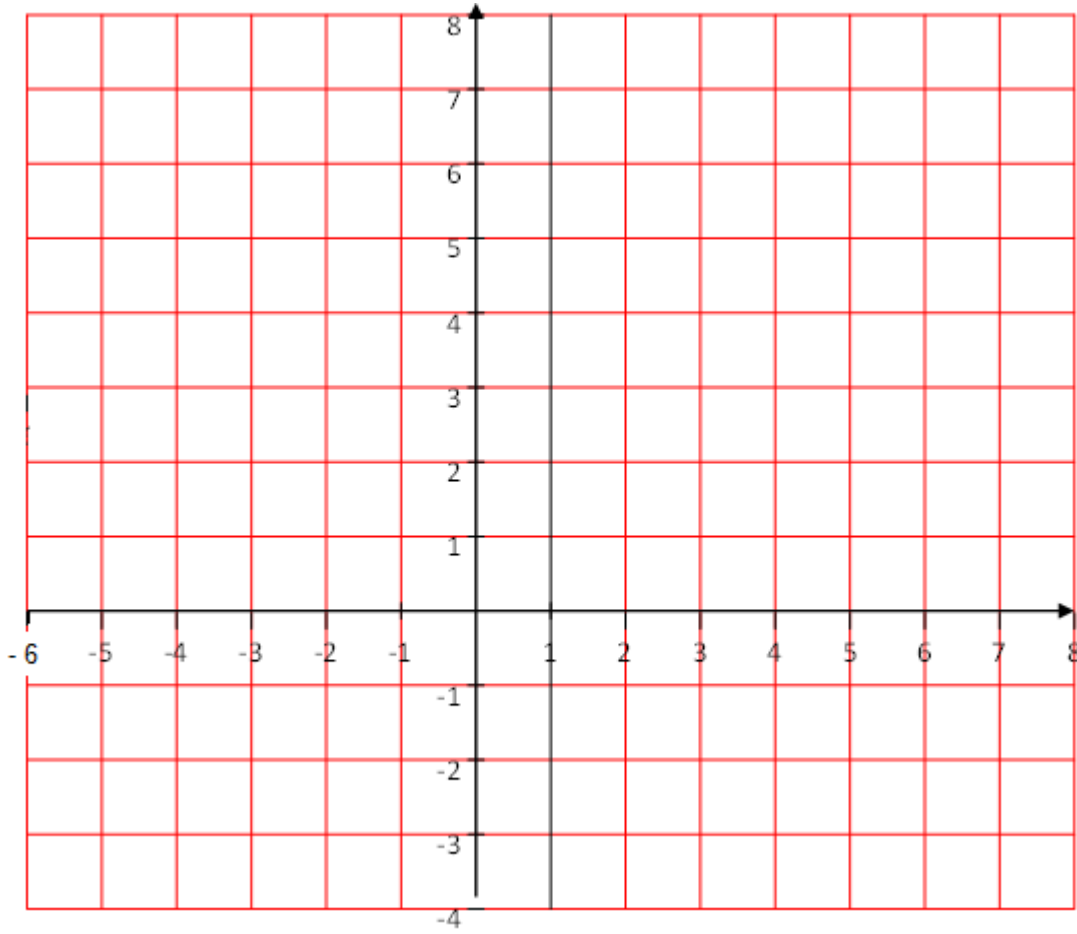
$$15\cos^2 x = 13 + \sin x$$

may be written as a quadratic equation in $\sin x$.

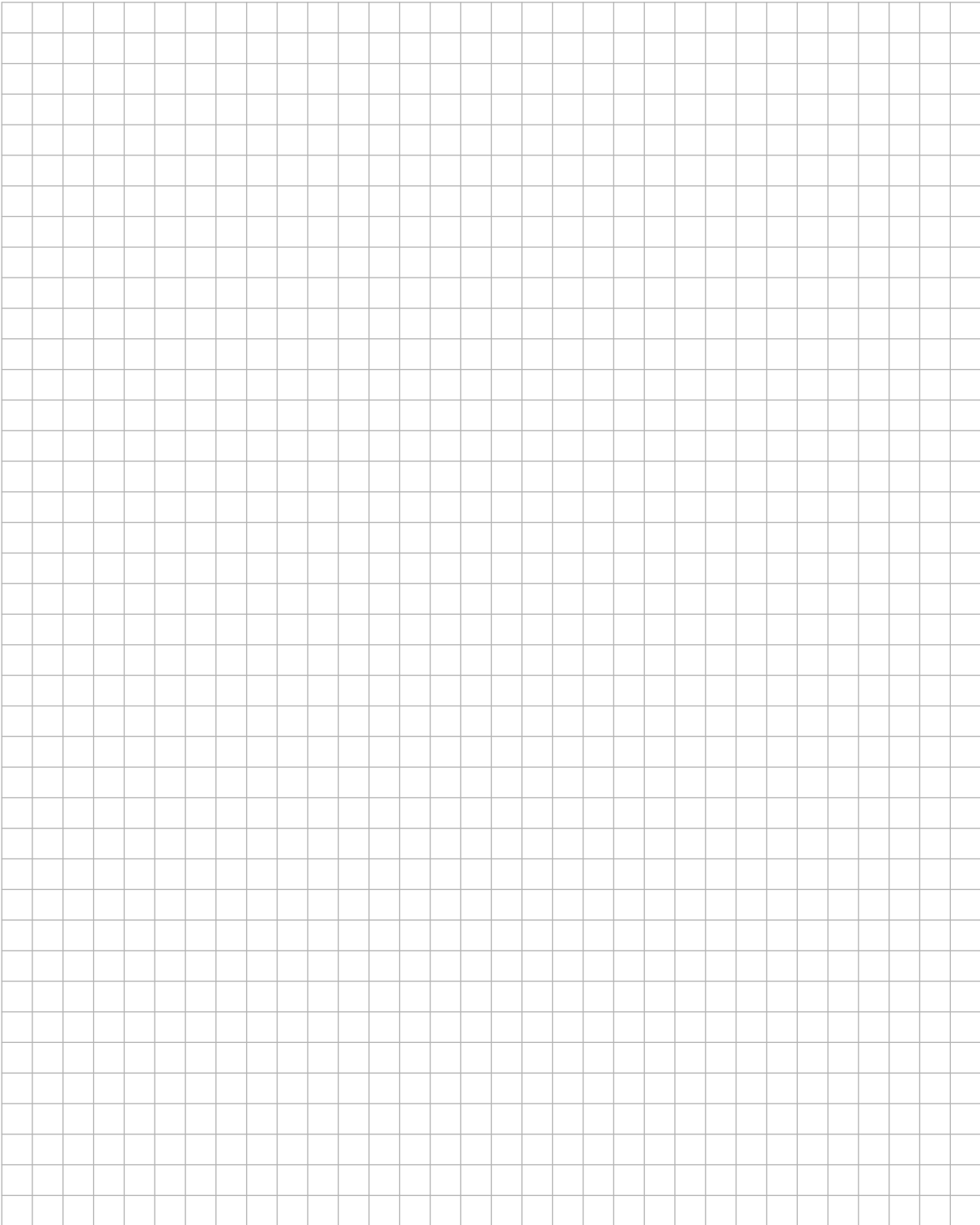
- (b) Solve the quadratic equation for $\sin x$, and hence solve for all values of x where $0^\circ \leq x \leq 360^\circ$.
Give your answer(s) correct to the nearest degree.

Question

- (a) On the grid provided draw circle p whose equation is $x^2 + y^2 - 4x - 2y - 5 = 0$.

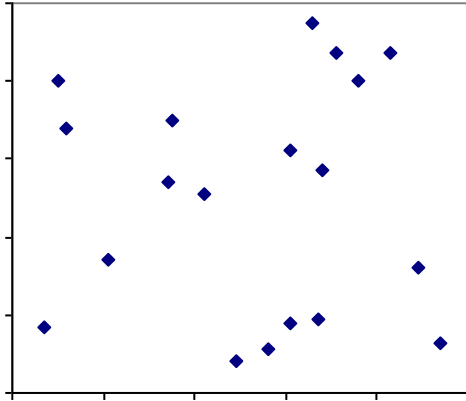


(b) Use **two different** methods to determine whether the line $l: 3x + y + 3 = 0$ is tangent to this circle p .

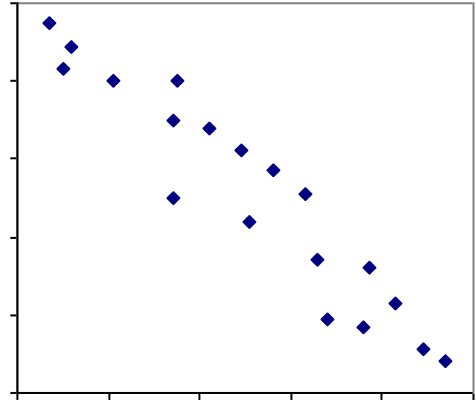


Question

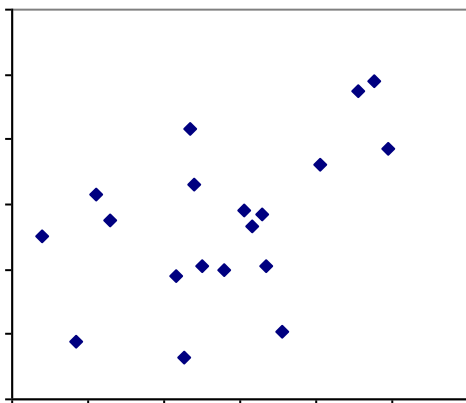
(a) For each of the four scatter plots below, estimate the correlation coefficient.



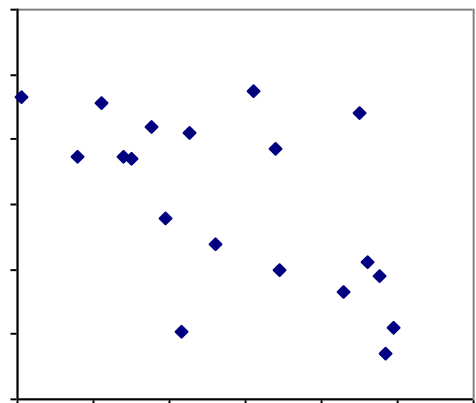
Correlation \approx



Correlation \approx



Correlation \approx



Correlation \approx

(b) Using your calculator, or otherwise, find the correlation coefficient for the data given in the table.

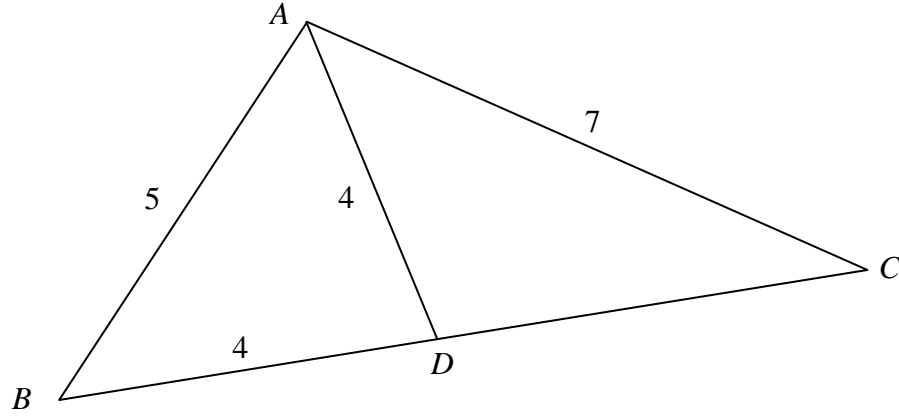
Give your answer correct to two decimal places.

x	y
0.0	0.5
5.0	1.3
5.2	3.3
6.1	6.7
9.3	4.5
9.5	4.6
9.9	6.5

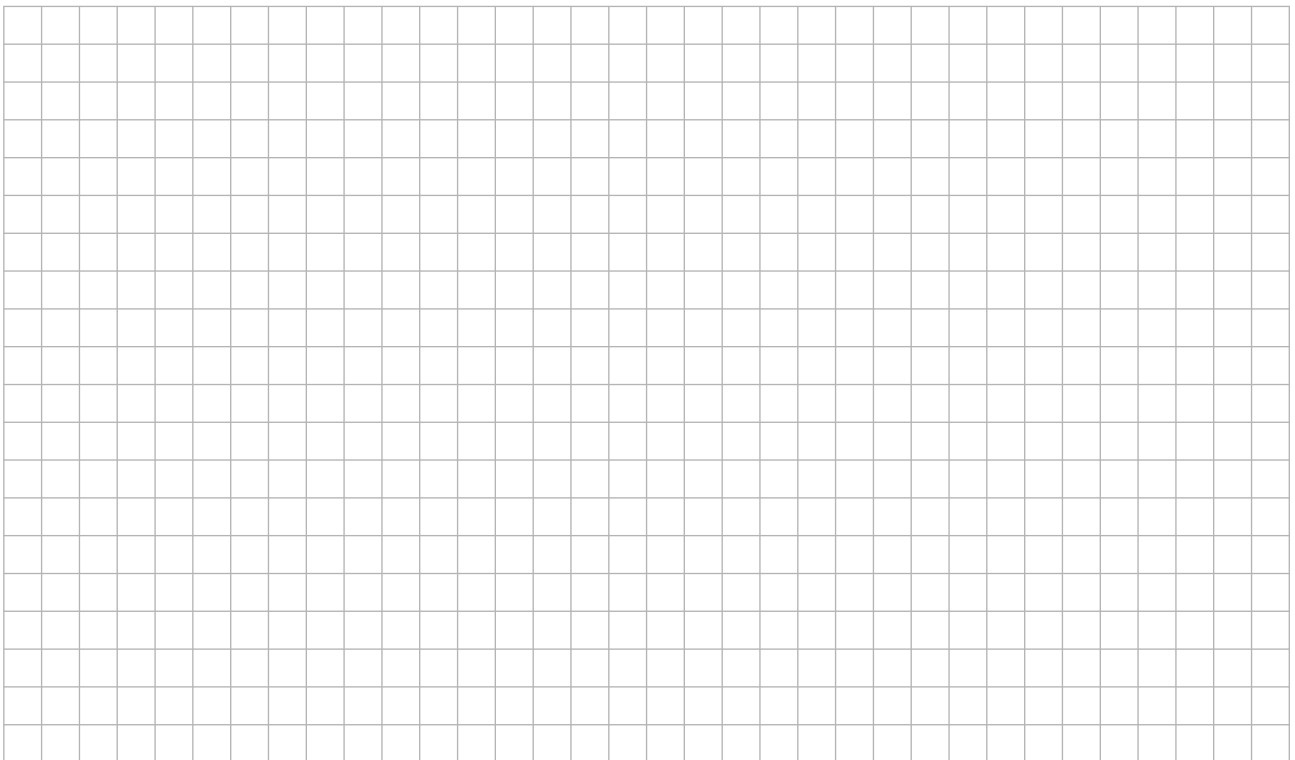
Answer:

Question

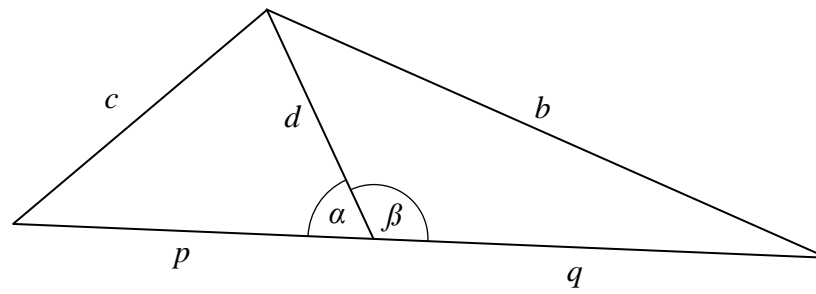
- (a) ABC is a triangle, and D is a point on $[BC]$.
The lengths $|AB|$, $|AD|$, $|AC|$ and $|BD|$ are as shown in the diagram.



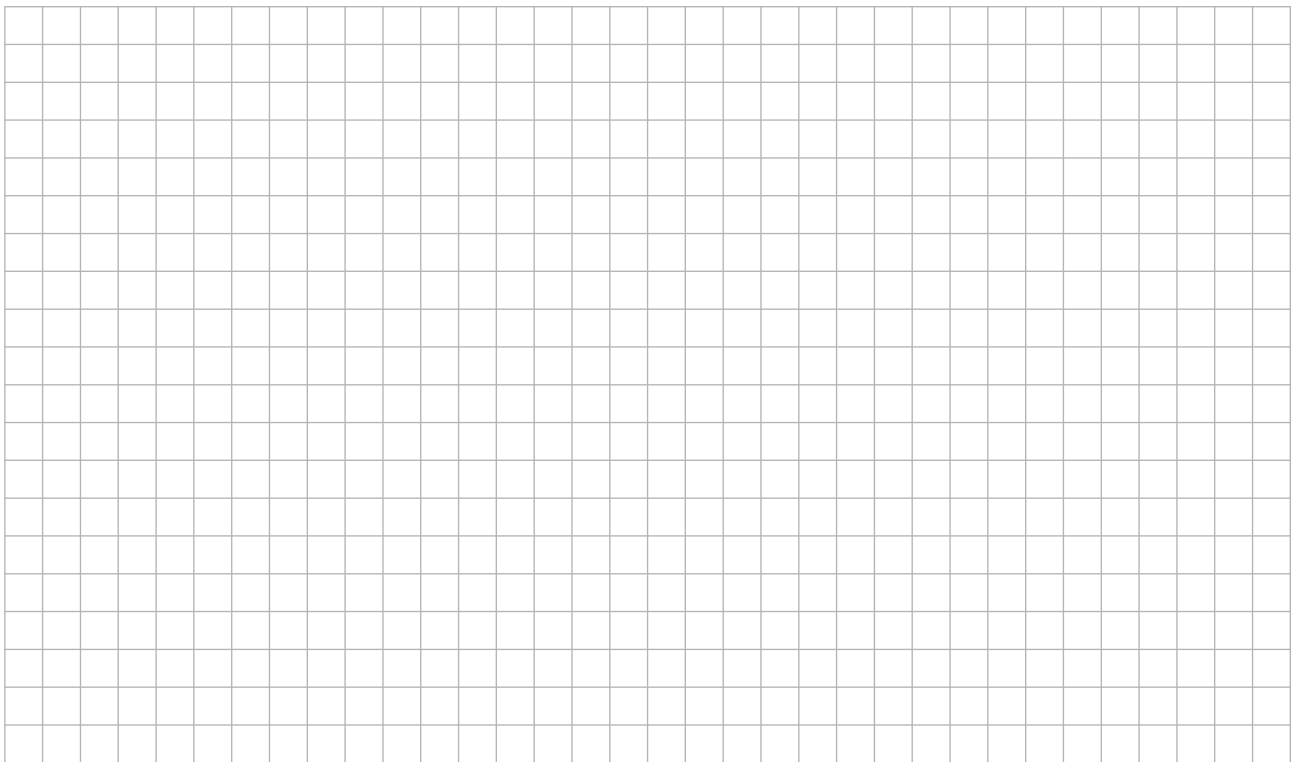
Find $|DC|$, correct to one decimal place.



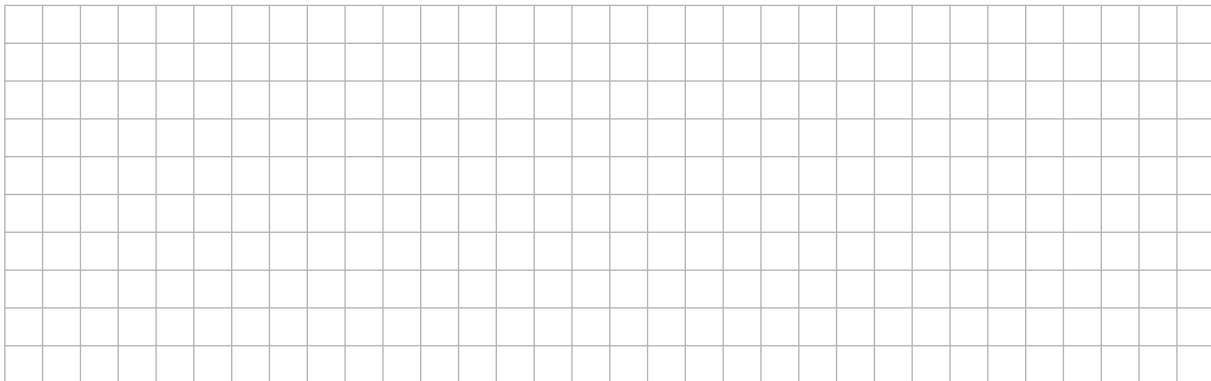
(b) Consider the diagram below.



Express $\cos \alpha$ and $\cos \beta$ in terms of the labelled lengths



(ii) Show that $pb^2 + qc^2 = (p+q)pq + d^2$



(ii) Find the probability that Laura hits the target fewer than nine times.

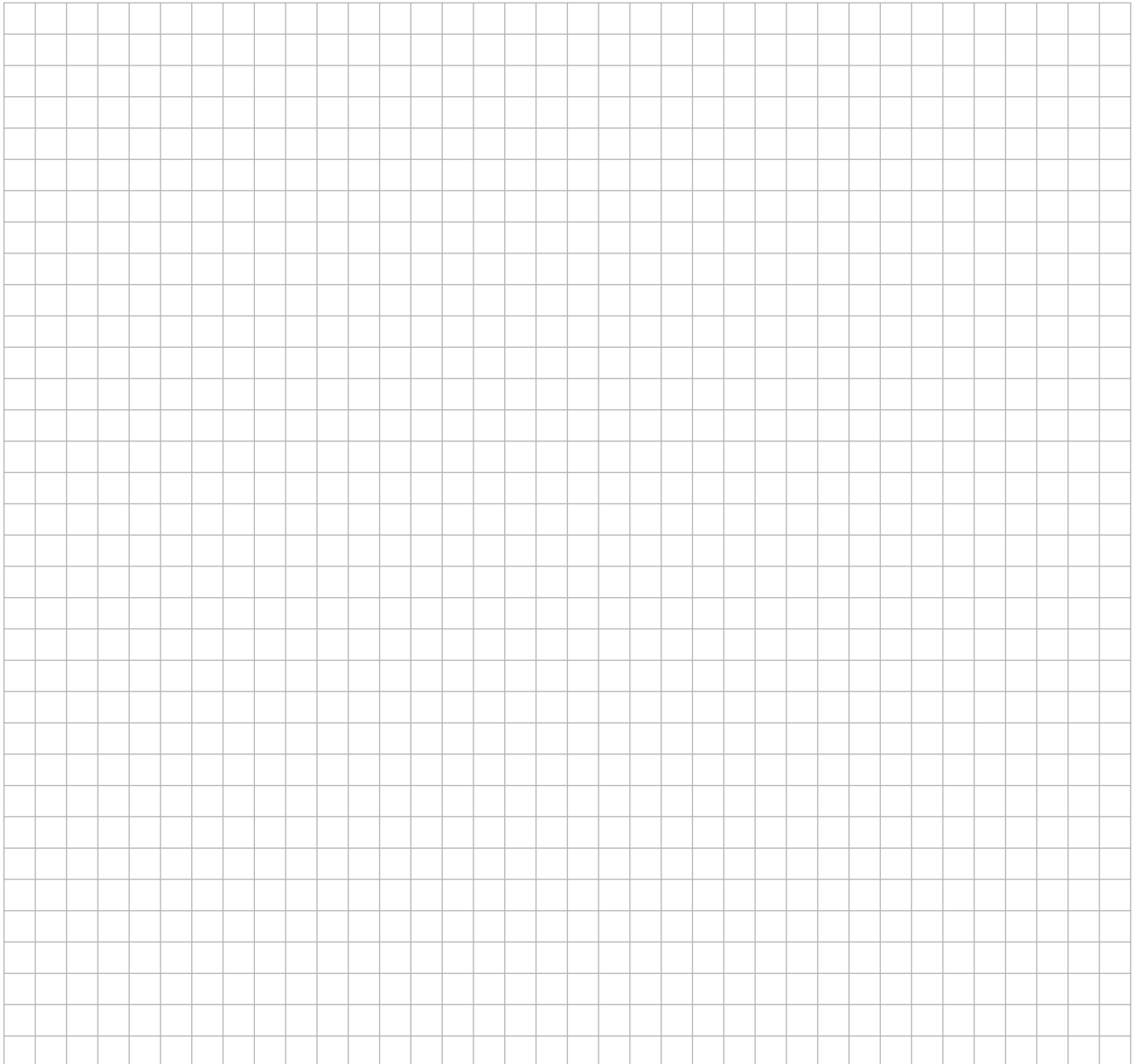
Give your answer correct to three decimal places.



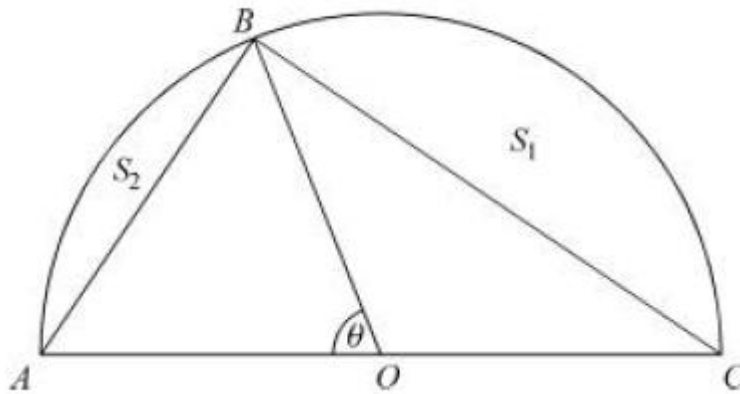
Question

You work for a market research company and you have been asked to find out the percentage of small and medium sized Irish companies that have email and internet access. Describe how you would find out this information.

In your answer, you should mention the **population**, the **sampling frame**, how you would select a **sample**, the **size of the sample** you would select and why you would choose this sample size. You should describe how you will gather the data and the potential **biases** you may encounter.

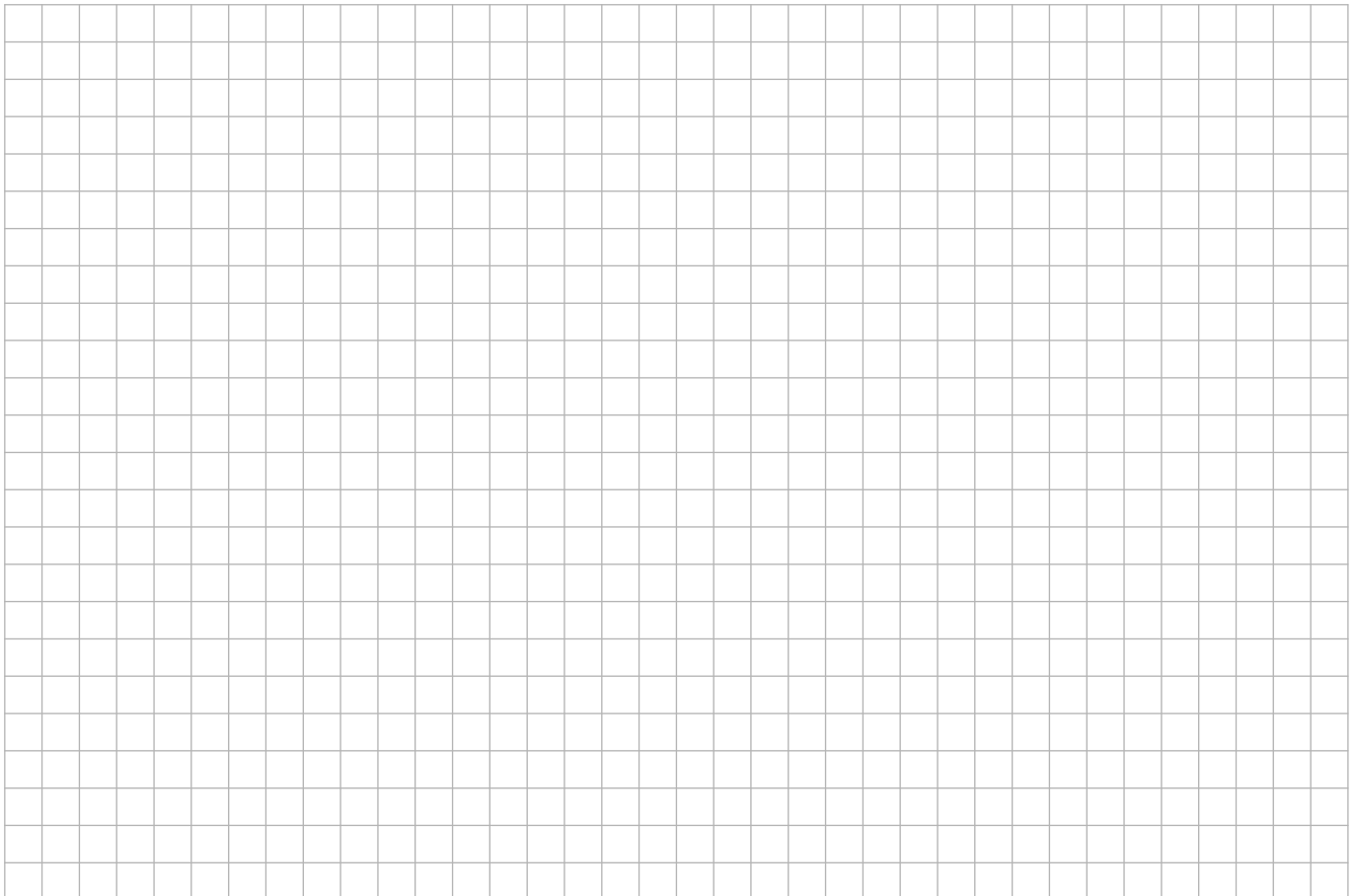
A large grid of graph paper, consisting of 20 columns and 30 rows of small squares, intended for writing the answer to the question.

Question



The diagram shows a semicircle ABC on $[AC]$ as diameter. The mid-point of $[AC]$ is O , and angle $AOB = \theta$ radians, where $0 < \theta < \frac{\pi}{2}$. The area of the segment S_1 cut off by the chord BC is twice the area of the segment S_2 bounded by the chord AB .

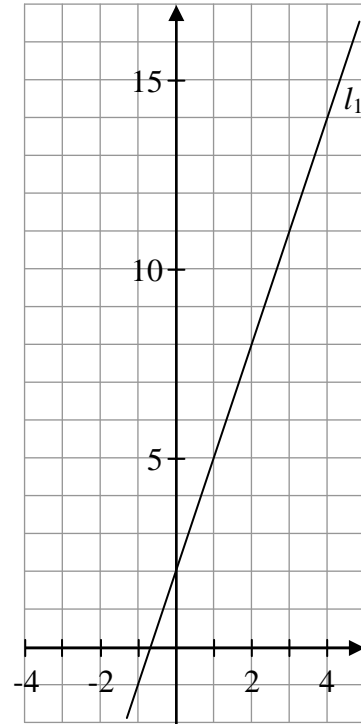
Show that $3\theta = \pi + \sin \theta$



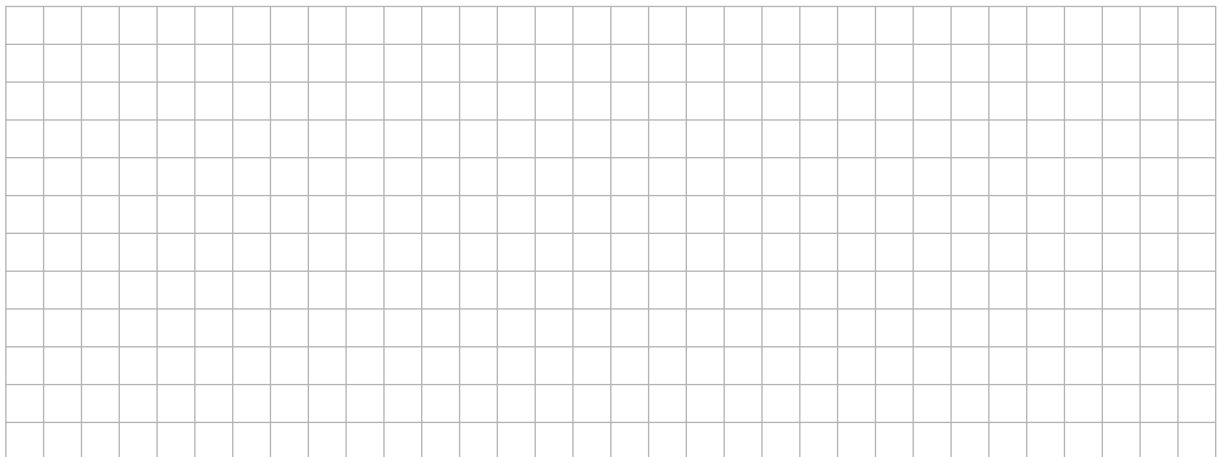
Question

The line l_1 in the diagram has slope 3 and y-intercept 2.

- (a) Write down the equation of this line, in the form $y = mx + c$.
- (b) On the diagram, draw and label the lines l_2 and l_3 , where:
 - l_2 has slope 3 and y-intercept 7
 - l_3 has slope 1 and y-intercept 8.



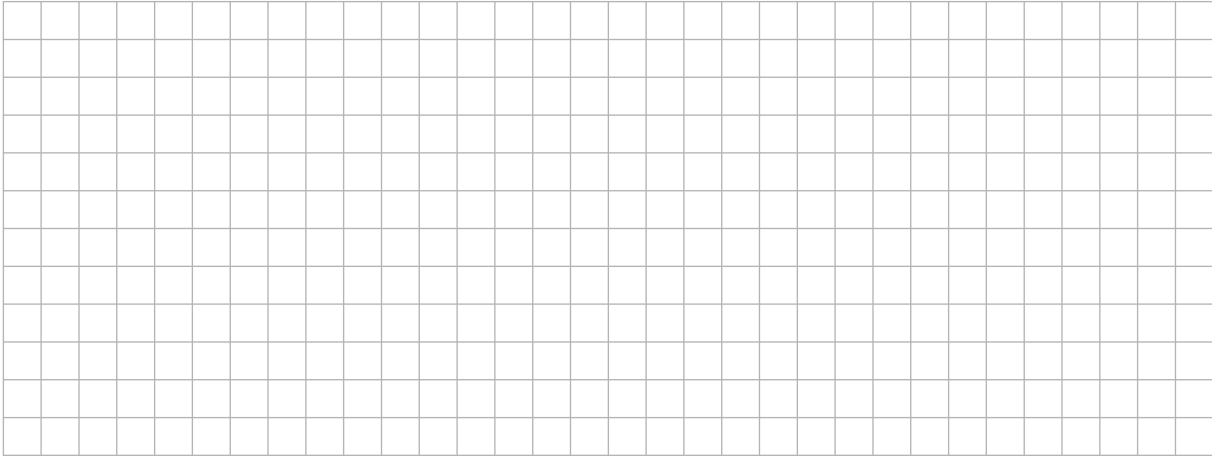
- (c) On the diagram, draw and label the line l_4 , which is perpendicular to l_1 and passes through the point $(0, 4)$.
- (d) Determine whether l_4 passes through the point $(27, -4)$.



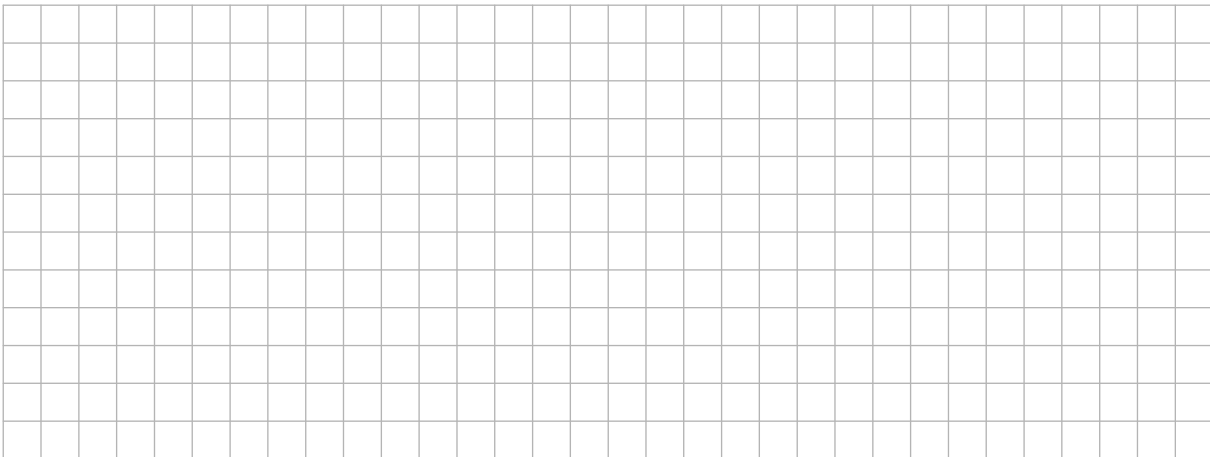
Question

P is the point $(0, 7)$ and Q is the point $(8, 11)$.

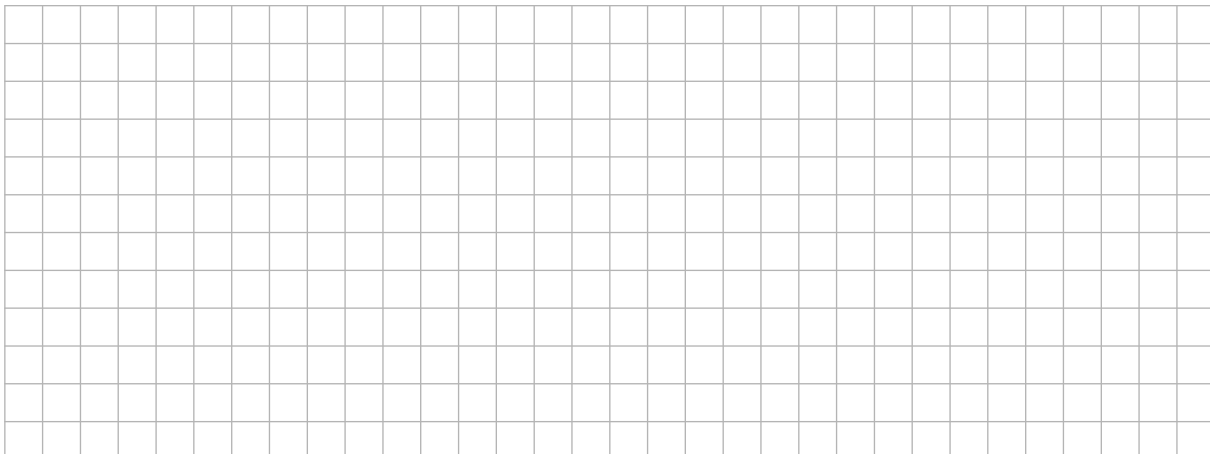
- (a) Find the equation of the circle with diameter PQ .



- (b) Find the equation of the tangent at Q .



- (c) This tangent crosses the x -axis at the point R . Find the co-ordinates of R .



Question

20% of the bolts produced by a machine are defective.

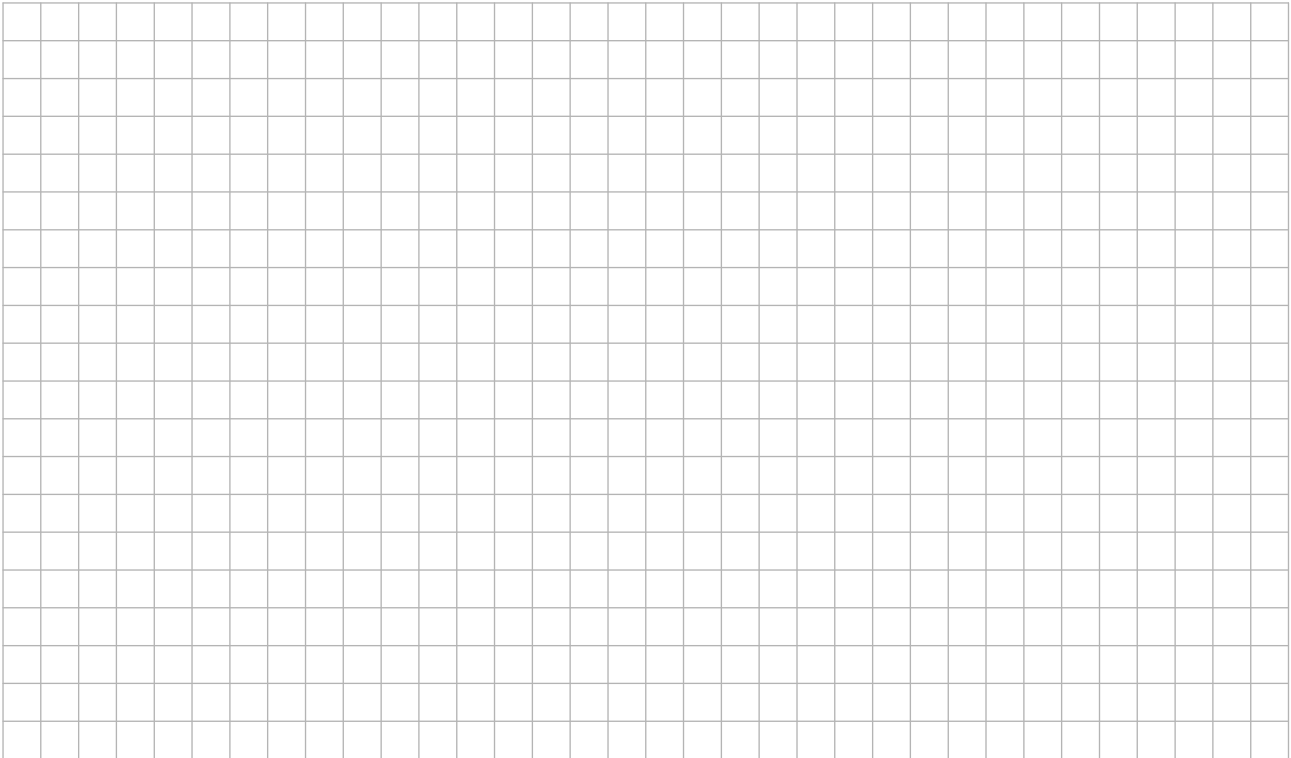
- (a) Find the probability that, in a group of five bolts randomly selected from a batch produced by the machine, at most two are defective.

- (b) A shipment of 250 packets of 5 bolts produced by this machine is inspected. A packet is rejected if it has more than two defective bolts. Show that approximately 14 packets are expected to be rejected.

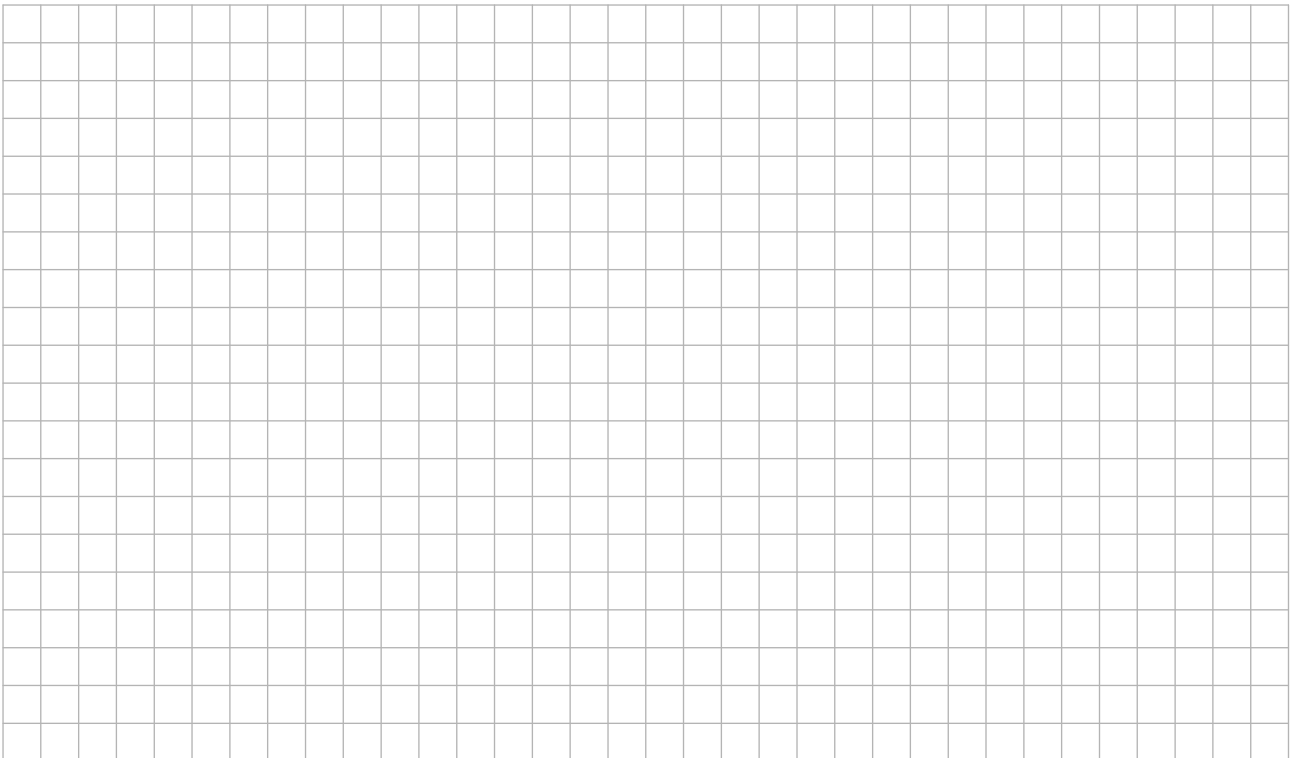
Question

ABC is an equilateral triangle inscribed in a circle centre O . A radius is drawn from O through the midpoint of AB to meet the circumference of the circle at D .

(a) Construct this diagram accurately, showing all construction marks.



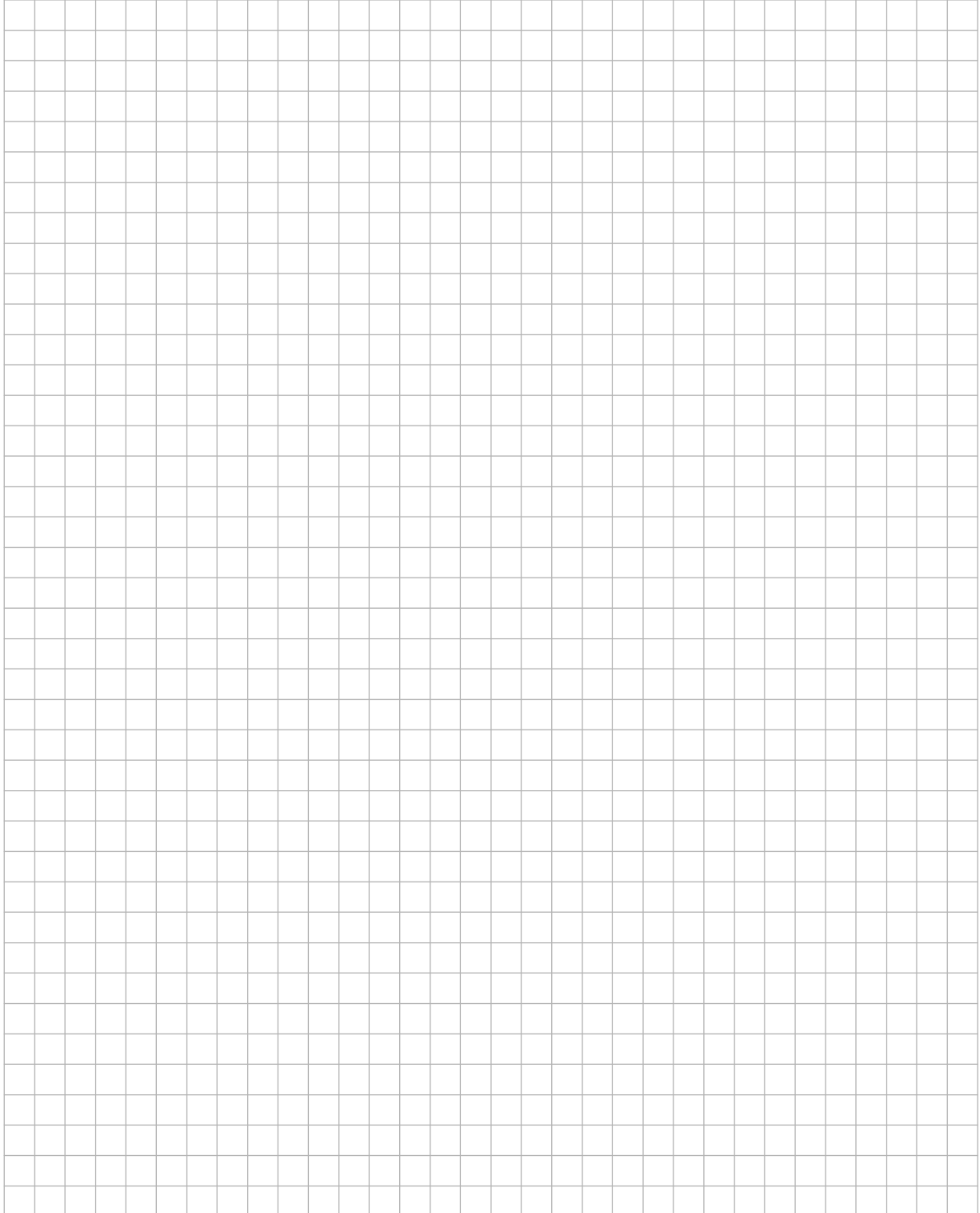
(b) Prove that ODA is equilateral.



Question

ABC is an isosceles triangle such that $|AB| = |AC|$ and D is a point on AB such that $CD \perp AB$.
Represent this on a diagram.

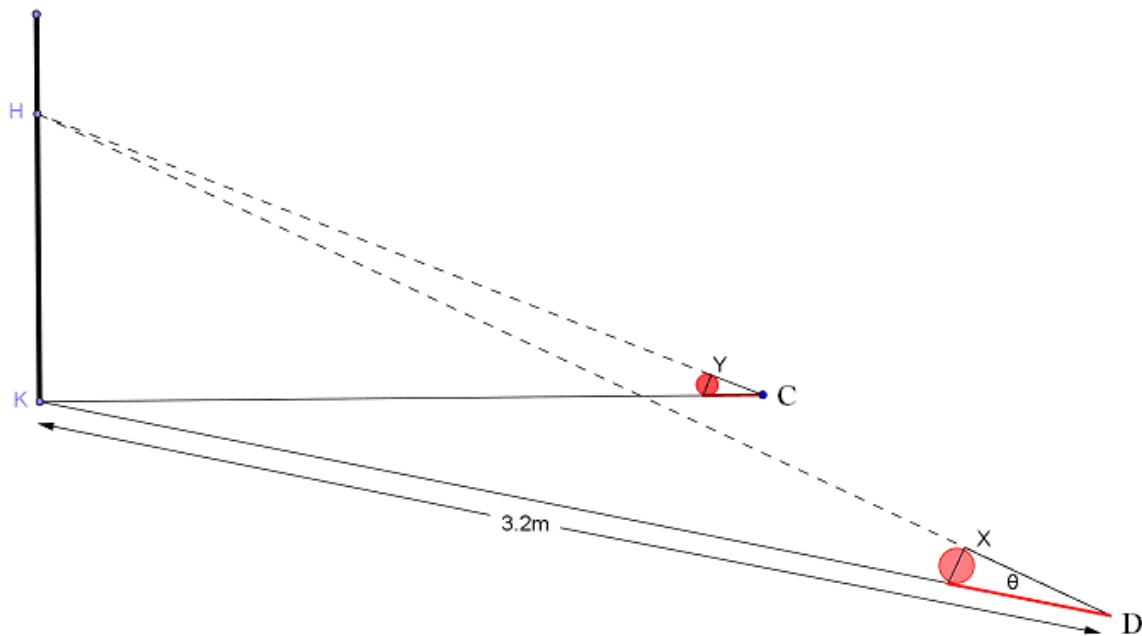
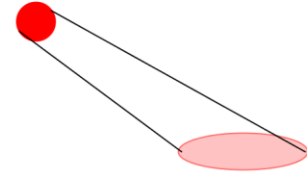
Show that $|\angle BCD| = \frac{1}{2} |\angle BAC|$



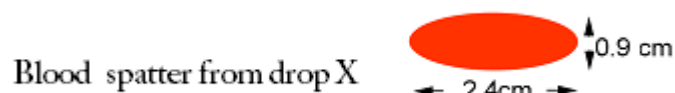
Question

(a) Forensic investigators encounter crime scenes containing traces of blood. A spherical drop of blood makes an elliptical spatter when it hits the ground at an angle.

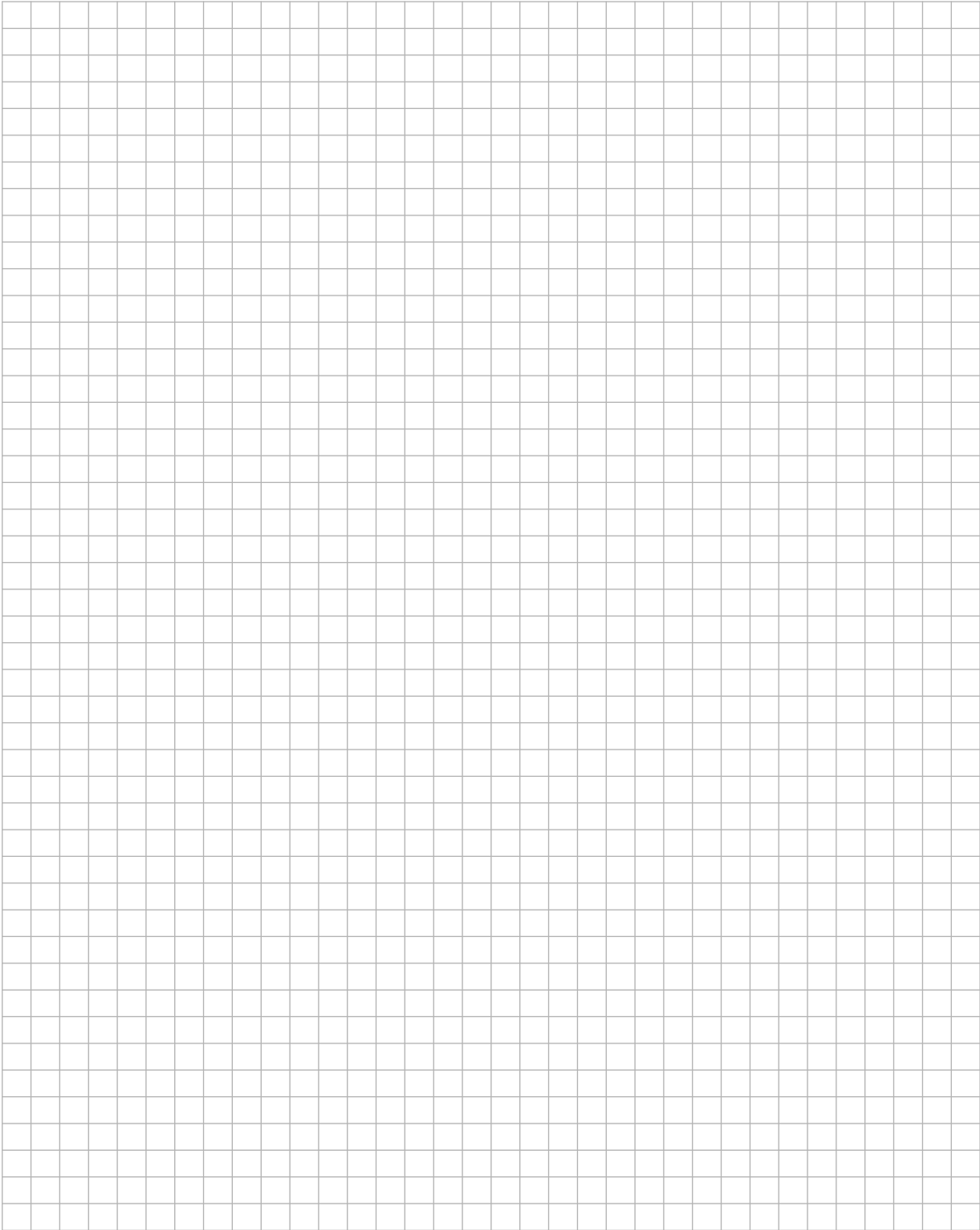
Investigators have mapped out the crime scene below showing two blood spatters on the floor at C and D. They measure a spatter in order to calculate the angle of impact and trace this back to an approximate starting place (assuming the blood drops travel in a straight line).



Since they know the drop started as a sphere, the width of the spatter drop will be the same as its diameter. They record the measurements of the blood spatter X:



Estimate the victim's height given that the blood originated from a chest wound. Show all your working and state any assumptions you make.



Question

- (a) In a component factory, machine A produces 30% of the output, machine B 25% and machine C the remainder.

Over a period of time, 1% of the output from machine A is found to be defective, 1.2% from machine B and 2% from machine C.

- (i) On a given day, the three machines produce a total of 10,000 components. How many components are likely to be defective?

- (ii) A quality controller selects a component at random from that day's output and finds that it is defective. What is the probability that this component was produced by machine B?

Question

Some research was carried out into the participation of girls and boys in sport. The researchers selected a simple random sample of fifty male and fifty female teenagers enrolled in GAA clubs in the greater Cork area. They asked the teenagers the question: *How many sports do you play?*

The data collected were as follows:

Boys	Girls
0, 4, 5, 1, 4, 1, 3, 3, 3, 1,	3, 3, 3, 1, 1, 3, 3, 1, 3, 3,
1, 2, 2, 2, 5, 3, 3, 4, 1, 2,	2, 2, 4, 4, 4, 5, 5, 2, 2, 3,
2, 2, 2, 3, 3, 3, 4, 5, 1, 1,	3, 3, 4, 1, 6, 2, 3, 3, 3, 4,
1, 1, 1, 2, 2, 2, 2, 2, 3, 3,	4, 5, 3, 4, 3, 3, 3, 4, 4, 3,
3, 3, 3, 3, 3, 3, 3, 3, 3, 3	1, 1, 3, 2, 1, 3, 1, 3, 1, 3

(a) Display the data in a way that gives a picture of each distribution.

A large grid of graph paper, consisting of 20 columns and 20 rows, provided for plotting the data distributions.

(b) State **one difference** and **one similarity** between the distributions of the two samples.

Difference:

Similarity:

(c) Do you think that there is evidence that there are differences between the two populations?
Explain your answer.

Note: you are not required to conduct a formal hypothesis test.

Answer: _____

Justification:

(d) The researchers are planning to repeat this research on a larger scale. List **two** improvements they could make to the design of the research in order to reduce the possibility of *bias* in the samples. Explain why each improvement you suggest will reduce the likelihood of bias.

Question

The *Wonder Building* is an arched building that does not need any support inside, due partly to the fact that its shape is an arc of a circle.

The photograph shows a *Wonder Building* being used in Antarctica.



The arc for a *Wonder Building* can be a full semicircle or less than a semicircle. It cannot be more than a semi-circle. The “span” of the building is the total width from one side of the arch to the other.

- (a) A particular *Wonder Building* has a span of 30 metres and a height of 10 metres.
Find the radius of the arc.



- (b) A customer wants a building with a span of 18 metres and a height of 10 metres.
(i) What arc radius would be required to give such a building?



(ii) Explain why the *Wonder Building* that the customer wants is not possible.



(c) An air force needs a *Wonder Building* to house a *Tornado* military jet.

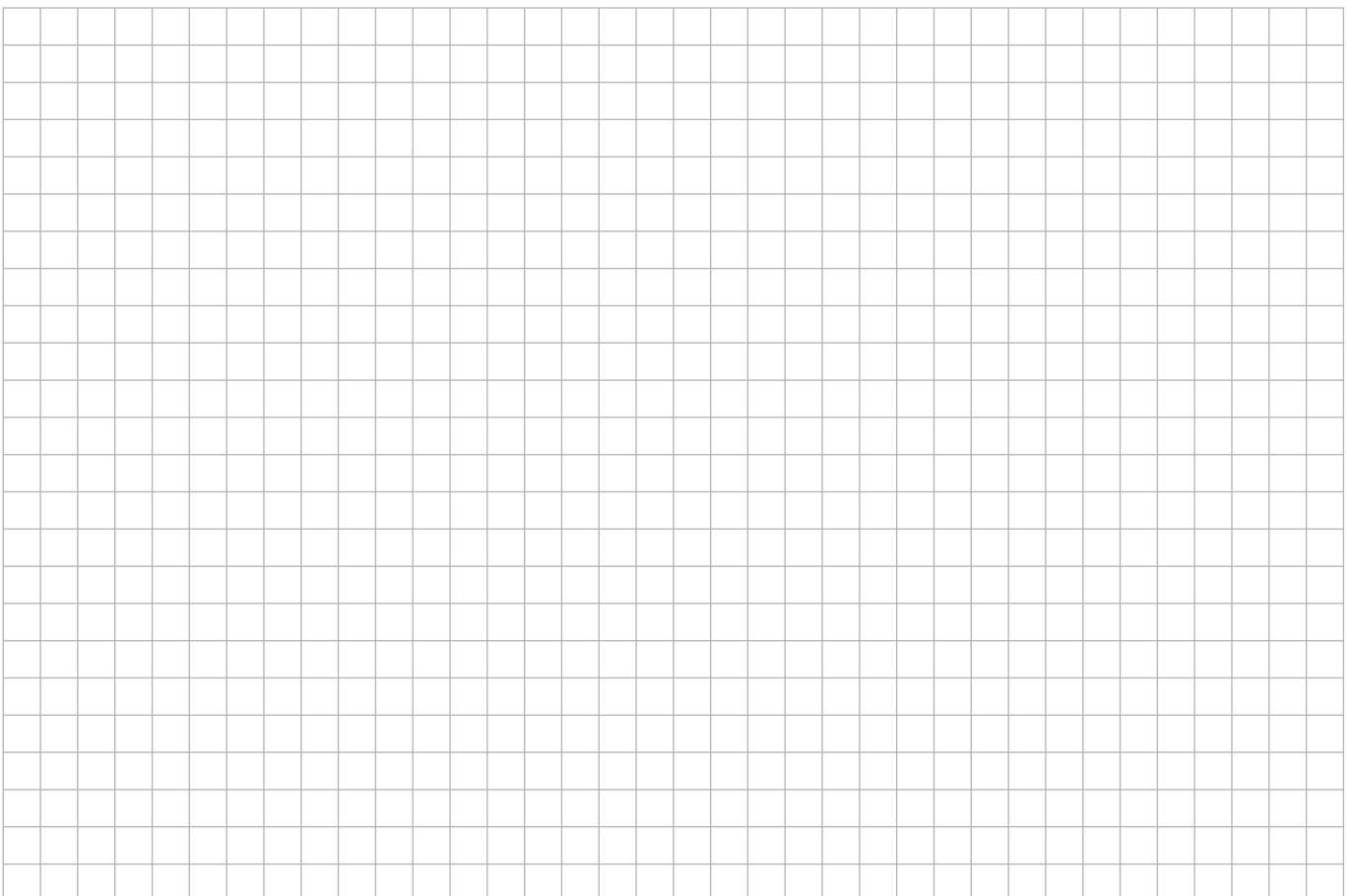
The dimensions of the aircraft are as follows:

- Wingspan: 14 metres
- Height: 6 metres
- Height of wingtips above ground: 2 metres.



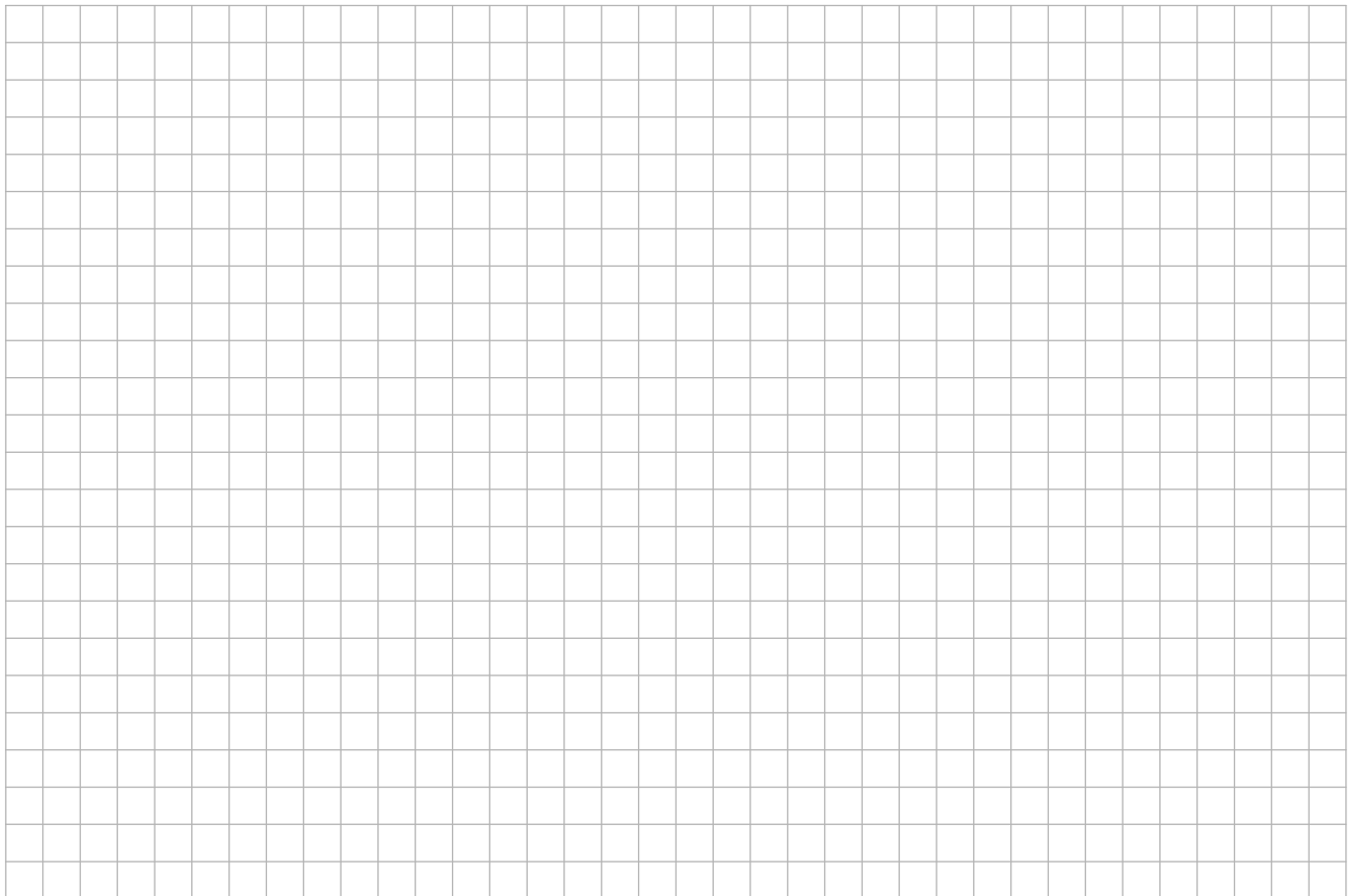
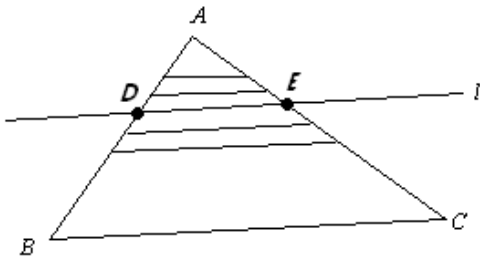
The shelter must be at least 0.5 metres above the top of the tail, and at least 1 metre clear horizontally of the wingtips.

For the shelter to have the exact clearance required, find the radius of the arc.



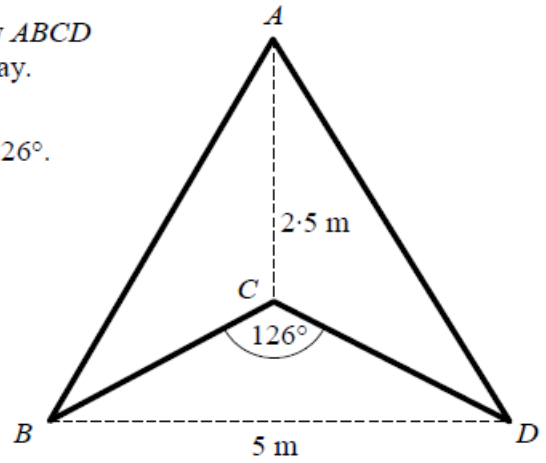
Question

- (a) Let $\triangle ABC$ be a triangle. The line l is parallel to BC and cuts $|AB|$ in the ratio $s:t$, where s and t are natural numbers. Prove that l also cuts AC in the ratio $s:t$.

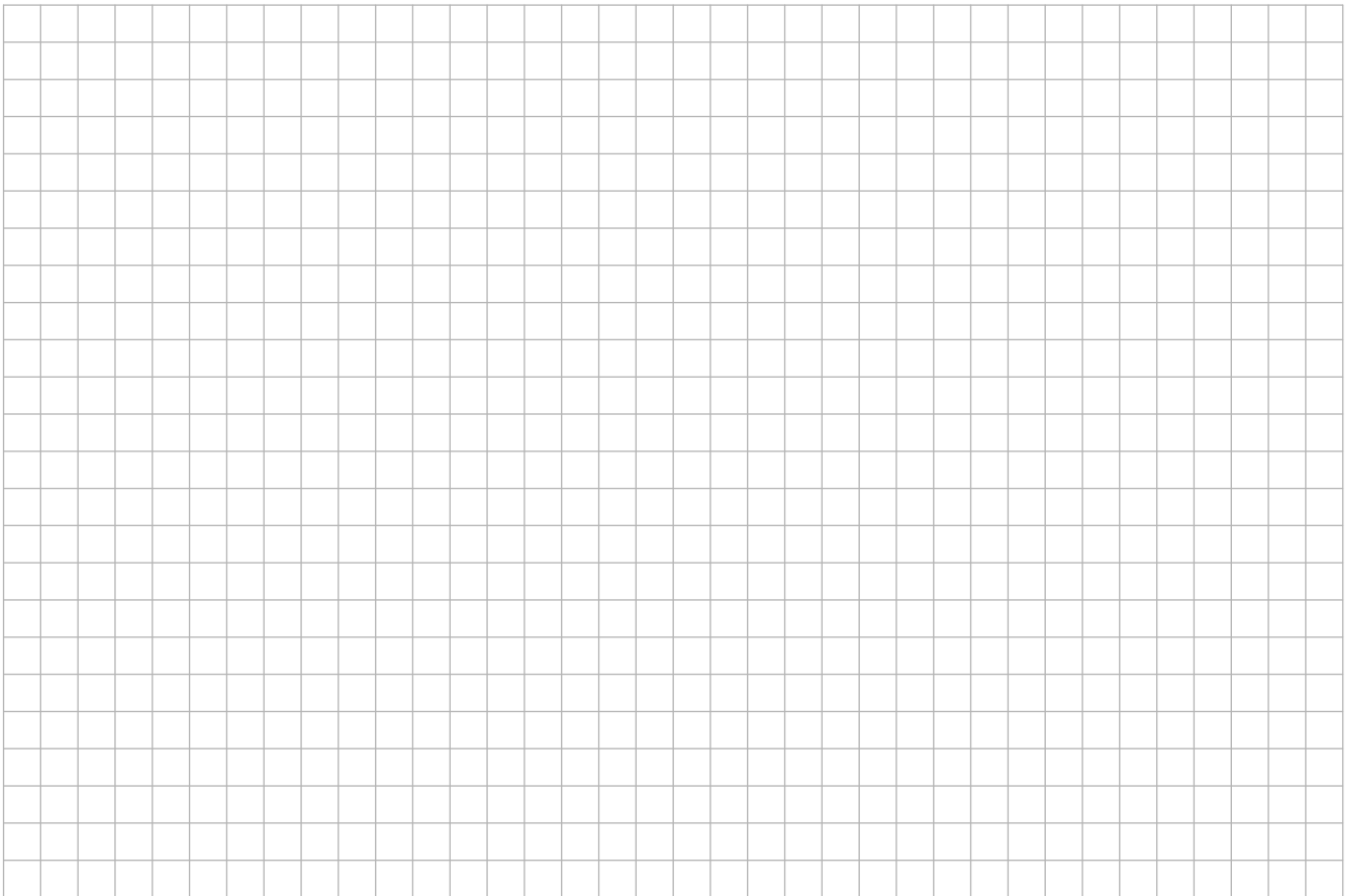


- (b) The diagram represents a large symmetrical arrow $ABCD$ that is painted on the ground at one end of a runway.

The distance BD is 5 metres and distance CA is 2.5 metres, as shown. The angle ADB measures 126° .



- (i) Find the length of the perimeter of the arrow.
Give your answer correct to one decimal place.



- (ii) *Cat's eyes* are reflective devices used in road markings. They are being laid along the perimeter of the arrow. One is placed at each vertex, and others are placed at intervals of no more than half a metre along the perimeter. How many are needed?

